

What is claimed is:

1. A method for projecting a superimposed image onto a target display surface under observation of at least one camera, the method comprising the steps of:

- 5           (a) determining a projective relationship between each of a plurality of projectors and the target display surface;
- (b) estimating a component image for each said projector, comprising:
- (1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain; and
- 10            (2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and
- (c) minimizing the difference between a sum of said component images and a frequency domain representation of a target image to produce a second component image for each said projector.
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2. The method of claim 1 wherein said step of minimizing the difference between said sum and said frequency domain representation of said target image comprises: (a) identifying a second set of frequency domain coefficients for use in producing a frequency domain representation of said second component image for a respective one of said projectors, and

20           (b) taking the inverse Fourier transform of said frequency domain representation of said second component image for said respective one of said projectors; and further comprising the step of projecting from each said projector, a respective one of said second component images to produce the superimposed image.

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3. The method of claim 1 wherein said step of determining a projective relationship further comprises:

- (a) observing the target display surface with the camera,  $\mathbf{c}$ ;
- (b) recovering a homography between each projector,  $\mathbf{p}_i$ , and the camera,  $\mathbf{H}_{\mathbf{p}_i}^{\mathbf{c}}$ , and
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4. The method of claim 2 wherein said step of using said projective relationship to determine said plurality of sub-sampled, regionally shifted images, comprises: **(a)** decomposing each said projective relationship,  $H_{pi}^b$ , into a linear shift matrix representing offsets between a respective of said projectors  $pi$ , and said reference frame  $b$ ; and **(b)** using said linear shift matrix for said determining said plurality of sub-sampled, regionally shifted images associated with said respective of said projectors  $pi$ .

5. The method of claim 1 wherein said step of minimizing the difference between said sum and said frequency domain representation of said target image,  $F_T[u, v]$ , comprises:

**(a)** minimizing the expression:

$$\left\| F_T[u, v] - \left( \sum_{i=0}^k F_{\Delta}^i[u, v] \right) \right\|^2$$

wherein  $k$  represents the total number of said plurality of projectors, said component image for each said projector is represented by  $F_{\Delta}^p[u, v] = \sum_{r=0}^N F_{\Delta r}[u, v]$ , and said sub-

sampled, regionally shifted images represented in the frequency domain are represented by  $F_{\Delta r}[u, v]$ , to identify a second set of frequency domain coefficients for use in producing a frequency domain representation of said second component image for a respective one of said projectors; and

**(b)** taking the inverse Fourier transform of said frequency domain representation of said second component image for said respective one of said projectors.

6. A system for projecting the superimposed image onto the target display surface, of claim 1, wherein: being projected from each said projector, is a respective one of said second component images to produce the superimposed image.

7. A method for projecting a superimposed image onto a target display surface under observation of at least one camera, the method comprising the steps of:

**(a)** determining a projective relationship between each of a plurality of projectors and the target display surface;

**(b)** estimating a component image for each said projector, comprising:

(1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain, and

(2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and

(c) performing an optimization using said component images and a frequency domain representation of a target image to produce a second component image for each said projector.

8. The method of claim 7 wherein:

(a) said step of performing an optimization comprises minimizing the difference between a sum of said component images and said frequency domain representation of said target image,  $F_T[u, v]$ , to produce said second component image for each said projector; and

(b) said step of determining a projective relationship further comprises:

(1) observing the target display surface with the camera,  $c$ ;

(2) recovering a homography between each projector,  $p_i$ , and the camera,  $H_{p_i}^c$ ; and

(3) using said homography,  $H_{p_i}^c$ , determine said projective relationship,  $H_{p_i}^b$ , wherein  $b$  represents a reference frame for the target display surface.

9. The method of claim 8 wherein said step of performing an optimization comprises minimizing the difference between a sum of said component images and said frequency domain representation of said target image,  $F_T[u, v]$ , by minimizing the expression:

$$\left\| F_T[u, v] - \left( \sum_{i=0}^k F_{\Delta}^i[u, v] \right) \right\|^2$$

wherein  $k$  represents the total number of said plurality of projectors, said component image for each said projector is represented by  $F_{\Delta}^p[u, v] = \sum_{r=0}^N F_{\Delta^r}[u, v]$ , and said sub-sampled, regionally shifted images represented in the frequency domain are represented by  $F_{\Delta^r}[u, v]$ ,

to identify a second set of frequency domain coefficients for use in producing a frequency

domain representation of said second component image for a respective one of said projectors.

10. A system for projecting the superimposed image onto the target display surface, of claim 7, wherein: being projected from each said projector, is a respective one of said second component images to produce the superimposed image.

11. A computer executable program code on a computer readable storage medium for projecting a superimposed image onto a target display surface under observation of at least one camera, the program code comprising:

(a) a first program sub-code for determining a projective relationship between each of a plurality of projectors and the target display surface;

(b) a second program sub-code for estimating a component image for each said projector, said second program sub-code comprising instructions for:

(1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain; and

(2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and

(c) a third program sub-code for minimizing the difference between a sum of said component images and a frequency domain representation of a target image to produce a second component image for each said projector.

12. The program code of claim 11 wherein said frequency domain representation of said target image as  $F_r[u, v]$ , and said third program sub-code comprises instructions for:

(a) minimizing the expression:

$$\left\| F_r[u, v] - \left( \sum_{i=0}^k F_{\Delta}^i[u, v] \right) \right\|^2$$

wherein  $k$  represents the total number of said plurality of projectors, said component image for each said projector is represented by  $F_{\Delta}^p[u, v] = \sum_{r=0}^N F_{\Delta r}[u, v]$ , and said sub-sampled, regionally shifted images represented in the frequency domain are represented by  $F_{\Delta r}[u, v]$ , to identify a second set of frequency domain coefficients for

use in producing a frequency domain representation of said second component image for a respective one of said projectors; and

(b) taking the inverse Fourier transform of said frequency domain representation of said second component image for said respective one of said projectors.

13. A computer executable program code on a computer readable storage medium for projecting a superimposed image onto a target display surface under observation of at least one camera, the program code comprising:

(a) a first program sub-code for determining a projective relationship between each of a plurality of projectors and the target display surface;

(b) a second program sub-code for estimating a component image for each said projector, said second program sub-code comprising instructions for:

(1) using said projective relationship, for each of said component images determine a plurality of sub-sampled, regionally shifted images represented in the frequency domain; and

(2) composing each said component image using a respective plurality of said sub-sampled, regionally shifted images; and

(c) a third program sub-code for performing an optimization using said component images and a frequency domain representation of a target image to produce a second component image for each said projector.

14. The program code of claim 13 wherein:

(a) said third program sub-code comprises instructions for minimizing the difference between a sum of said component images and said frequency domain representation of said target image to produce said second component image for each said projector; and

(b) said first program sub-code comprises instructions for, while observing the target display surface with the camera,  $\mathbf{c}$ , recovering a homography between each projector,  $\mathbf{p}_i$ , and the camera,  $\mathbf{H}_{\mathbf{p}_i}^{\mathbf{c}}$ ; and using said homography,  $\mathbf{H}_{\mathbf{p}_i}^{\mathbf{c}}$ , determining said projective relationship,  $\mathbf{H}_{\mathbf{p}_i}^{\mathbf{b}}$ , wherein  $\mathbf{b}$  represents a reference frame for the target display surface.